

Kriptovaluták elméleti háttere (VITMDV04)

Hivatkozások / References

Ladóczki Bence – BME VIK TMIT

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